

DECUS NO.

8-169H

TITLE

DISTANCE AND BEARING

AUTHOR

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COMPANY

Submitted by: Joann E. Gavan Atlantic Oceanography Laboratory Bedford Institute Dartmouth, Niva Scotia, Canada

DATE

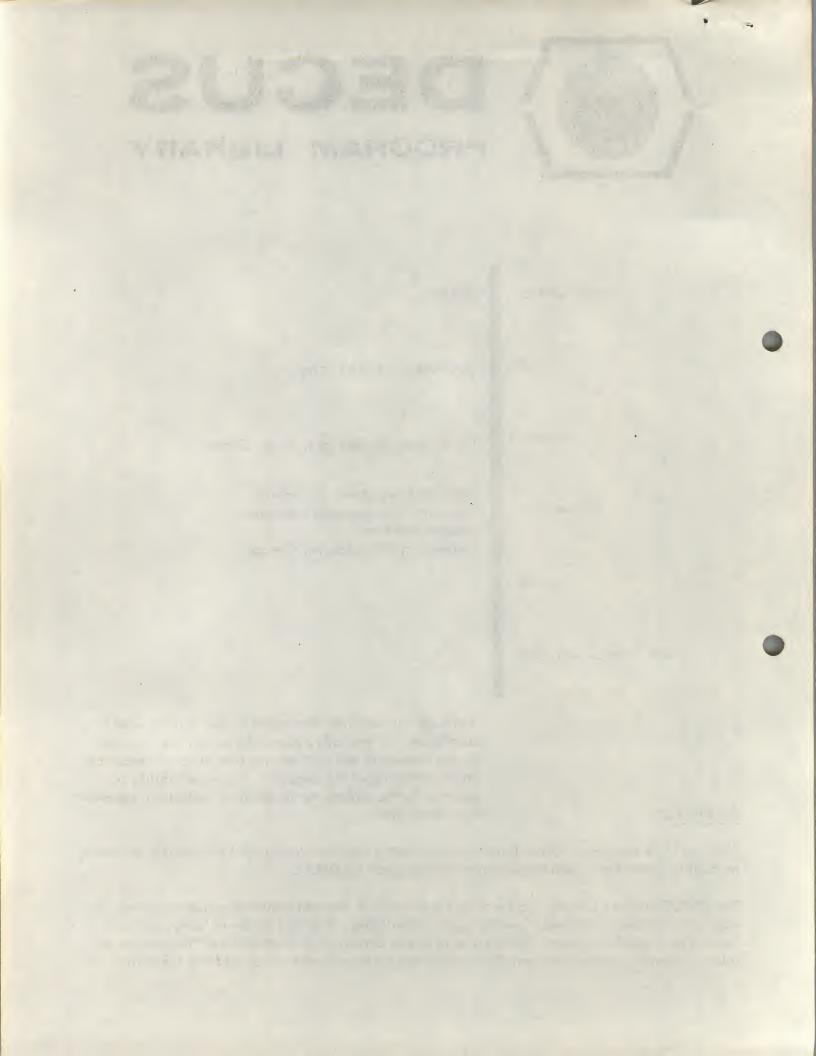
SOURCELANGUAGE

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IDENTIFICATION

- 1.1 Number: OCDA-8-08 (P-08-01) 1.2 Title: DISTANCE AND BEARING
- 1.3 Date: May 1968 1.4 Computer: PDP-8
- 1.5 Language: PAL III

2. ABSTRACT

The distance and bearing are calculated for two positions specified by their latitudes and longitudes.

3. REQUIREMENTS

- 3.1 Storage: 5 - 7, 40 - 104, 200 - 577, 4600 - 7577
- 3.2 Subprograms and/or Subroutines
- 3.2.1 F.P. Package (Digital 8-5D-S)
- 3.3 Equipment: Teletype

4. USAGE

- 4.1 Loading: The Binary Loader (Digital-2-U) is used to load the F.P. Package followed by the program.
- 4.2 Calling Sequence: N/A
- Switch Settings: N/A 4.3
- Start up and/or Entry: The program is started at loc. 200g. Then the 4.4 positions are typed on the teletype.
- 4.5 Errors in Usage and Recovery: A space is the only legal terminating character. If any other terminating character is read, the preceding number is ignored, (i.e. all digits typed between the last space and the illegal terminating character). To continue it is necessary to retype the number.
- RESTRICTIONS N/A

6. DESCRIPTION

- Discussion: The program calculates the distance and bearing between 6.1 positions. Initially the program requires two positions, but only one thereafter. The distance and bearing between the last two stations typed are calculated. All I/O is on the teletype.
- 6.2 Examples and/or Applications: Given in Fig. 1

7. METHODS

7.1 Discussion: N/A

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      23.8
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      28.2

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      15.5
      63
      19.5
      +0019.24
      +036.96

      43
      52.8
      62
      53.2
      +0054.78
      +039.87

      43
      28.8
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      27.2
      +0056.53
      +038.18

      43
      10.6
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      06.3
      +0043.98
      +039.98

      42
      50.8
      61
      44.1
      +0047.48
      +039.45
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7.2 Algorithm: The following equations are used to find the geodetic distance between two points given their latitudes and longitudes:

Sain
$$\alpha = \frac{\Delta \lambda \cos Q_m}{A_m} = U$$

$$S \cos \alpha = -\frac{\Delta Q \cos \Delta \lambda_2}{B_m} = V$$

$$A_m = \frac{\left(1 - e^2 \sin^2 Q_m\right)^{\frac{1}{2}}}{a \sin I''}$$

$$B_m = \frac{\left(1 - e^2 \sin^2 Q_m\right)^{\frac{3}{2}}}{a\left(1 - e^2\right) \sin I''}$$

- where $\lambda_{i,j}\lambda_{i}$: longitude of the two points
 - Φ. Q: latitudes of the two points
 - S: distance bwtween positions
 - Om: mean latitude
 - - e: eccentricity $e^2 = .0067686275$
 - a: equatorial semi-axis
 - b: polar semi-axis
 - sin I": permits Δλ to be expressed in seconds.

$$\Delta \lambda = \lambda_1 - \lambda_2$$

$$\Delta Q = Q_1 - Q_2$$

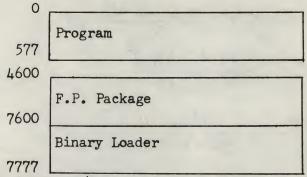
$$\frac{1}{a \sin i''} = .032559$$

$$\frac{1}{a (1-e^2) \sin I''} = .032559$$

- 8. FORMAT
- 8.1 Input Data: Each position is given by four numbers which represent the latitude and longitude in degrees and minutes. The terminating character for each number is a space.
- 8.2 Core Data: N/A
- 8.3 Output Data: The O/T record consists of the distance in kilometers and the bearing in degrees (+xxxx.xx +xxx.xx)). Note that if the bearing is a multiple of 90, a series of x's will be printed.
- 9. EXECUTION TIME N/A

10. PROGRAM

10.1 Core Map:



- 10.2 Dimension List: N/A
- 10.3 Macro, Parameter, and Variable List: This is included with the listing of the program.
- 10.4 Program Listing: Attached at the end of the program write-up.

11. DIAGRAMS

11.1 Flow Chart: Shown in Fig. 2

12. REFERENCES

- 12.1 Other Library Program:
- 12.1.1 F.P. Package (Digital 8-5D-S)
- 12.2 Digital Manuals:
- 12.2.1 F.P. Manual (Digital 8-5-S)
- 12.3 DECUS Programs:
- 12.3.1 Modification to Fixed Point O/T in the PDP-8 F.P. Package (Decus No. 8-44)
- 12.4 Textbooks:
- 12.4.1 U.S. Coast and Geodetic Special Publication #8

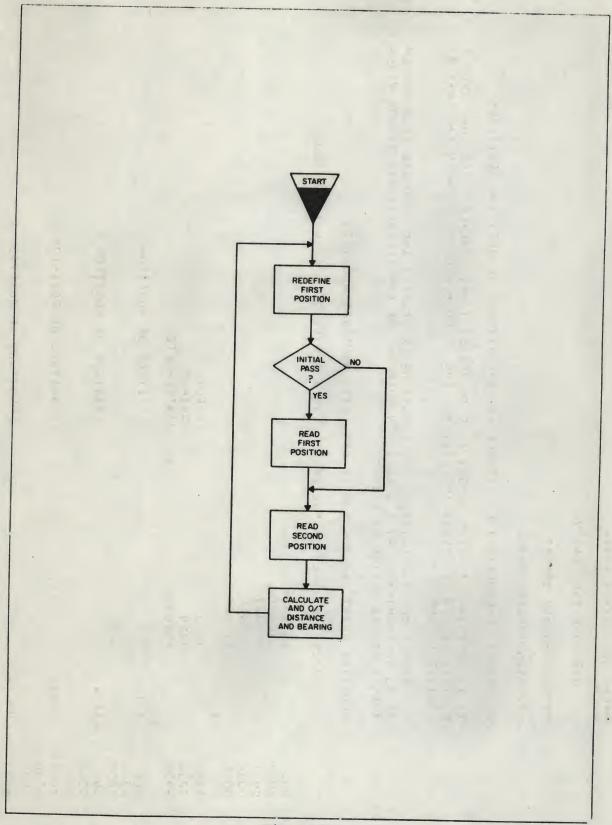


Figure 2

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/THE FORMAT FOR THE LATITUDE AND LONGITUDE IS DEGREES AND MINUTES. EACH NUMBER / IS TO BE TERMINATED BY A SYMBOL OTHER
                                            ALT IS NECESSARY TO TYPE 2 POSITIONS THE FIRST TIME, HOWEVER AFTER THAT ONLY I
                                                       APOSITION IS TO BE TYPED. THE DISTANCE AND AZIMUTH WILL BE BETWEEN THE LAST 2
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DISTANCE AND BEARING

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0075	0010	1010	2010	0103	0104	2010	0500	0500	0201	0202	0203	020	0205	0200	0201	0510	0211	0212	0213	9214	0215	0216	0217	0220	0221	0222	0223	0224	0225	0226	0227	0530	0231	0232	0233	0234	0235	0235	0237	0540	0541	

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STORE IN AM

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/E0((C-PI)003/2) /STORE IN BM 100S(A(LATI+LAT2))

/(LONGI-LONG2)

/CHECK ON SIGN, REQUIRE TO BE POS. /SUB TO CONVERT TO POS NUMBER

/FOABSF (LONGI-LONG2) OCOS(A(LATI+LAT2))

/U IS STORED IN LUC AM

/COS(A(LONGI-LONG2))

/(LATI-LATZ)

/CHECK ON SIGN, REQUIRE TO BE POS. /SUB TO CONVERT TO POS. NUMBER

/ABSF (LATI-LAT2) OF COS (A(LONGI+LONG2))

IS STORED IN LUC BM

/CHECK IF U=0

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/1/A(1-E002)SINI=.032559

/1/ASINI=.032339

/CONSTANT=1

/V=0, THEREFORE DISTANCE=U

/U/SIN(ARC TAN(U/V))
/STORE DISTANCE IN LOC BM

/SINCARC TANCU/VI)

/ARC TANCUIV)

/CHECK IF V=0

/U=0, THERFORE DISTANCE=V

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